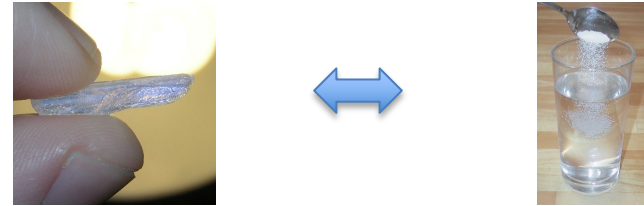
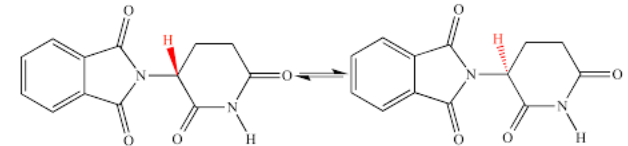


Drug Reactions and Transitions

- *Crystallization, Dissolution*



- Drug *Isomerization* to Active conformer

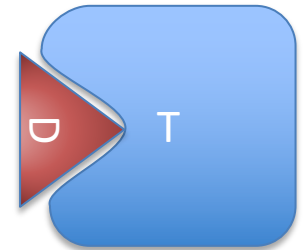
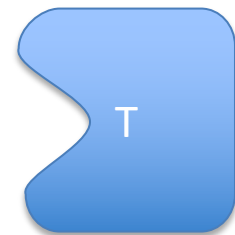
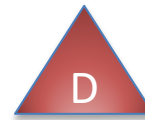


Thalidomide **R** ↔ Thalidomide **S**

- Drug *Binding* to its Target

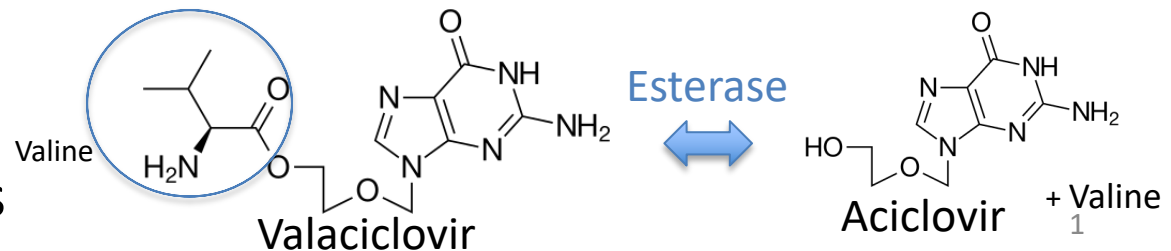


vs Dissociation



- *Chemical Transformations*

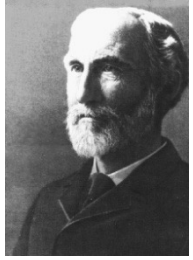
reactants ↔ products



- Many other examples

Thermodynamics in Pharmacology

Drug Discovery and Properties



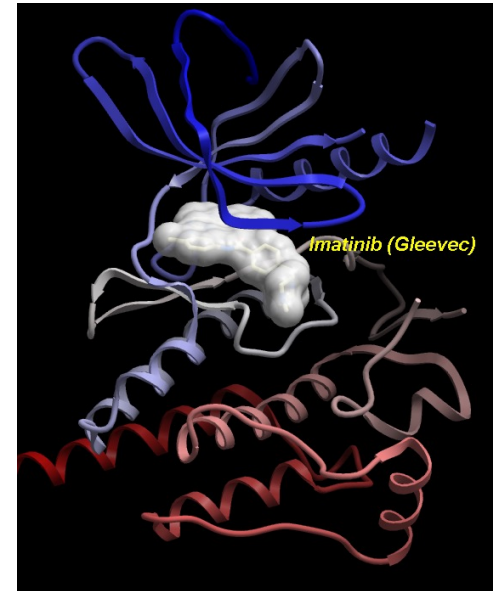
Most drugs act via **binding** specifically to a receptor. How do we find a **chemical structure** that binds to a receptor? What **concentration** is needed for a therapeutic effect?

$\Delta G_{\text{binding}}$: the median value for small drugs is ~ -11 kcal/mole. That corresponds to:
 $K_{\text{dissociation}} \sim 20$ nM. How is ΔG related to K ?

$$\Delta G_{\text{binding}} = \Delta G_{\text{complex}} - (\Delta G_{\text{ligand}} + \Delta G_{\text{target}})$$

What is **G** and ΔG ? How is it related to kinetic and potential energy of molecules? How to measure it?

Reactions and transitions, **Equilibria**, energies, concentrations,

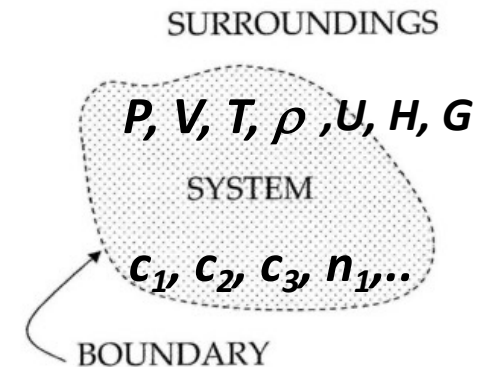


Thermodynamics. Part1. Enthalpy

- Drugs go through transitions and modifications, both physically and chemically.
- Transitions can reach **EQUILIBRIUM** in which the total **free energy function G** has the lowest value.
- **G** consists of **Enthalpic (H)** and Entropic terms
- Enthalpy, or **heat content**, grows with **T**
- The slope of **H vs T** curve is called **Heat Capacity**
- Properties of individual molecules are replaced by mean quantities for a very large number of molecules, called **Thermodynamic Variables**

Thermodynamics: System and variables

- Which quantities define a system?
Concentrations of constituents, Energy functions (internal energy **U**, enthalpy **H**, free energy **G**), **T**emperature, **P**ressure, **V**olume, ..
- **Extensive** quantities are proportional to the amount of substance (e.g., **V**, number of moles, energy)
- **Intensive** quantities are independent of the amount of substance (e.g., density ρ , temperature **T**, pressure **P**, concentrations)
- Intensive quantities are either intrinsically intensive (e.g., pressure), or are the ratio of two extensive quantities (e.g., density = mass/volume).
- Power of theory: Thermodynamics predicts the state of a complex system via only small number of variables of state.
 For example, to describe all properties of 1 g of water, only two variables of state are sufficient (e.g., **P** and **T**).
- **Equations of State:** relationship between variables (or quantities), e.g. **$PV = nRT$**



Type of system	Mass flow	Work	Heat
Open	✓	✓	✓
Closed	✗	✓	✓
Thermally isolated	✗	✓	✗
Mechanically isolated	✗	✗	✓
Isolated	✗	✗	✗

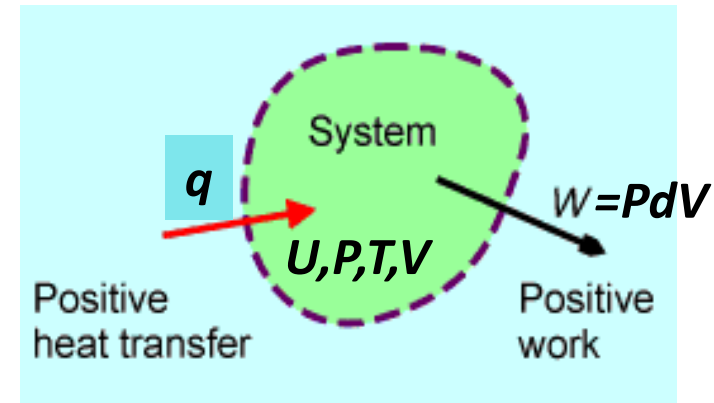
The First Law of Thermodynamics

- Conservation of Energy: “heat in” increases the energy, “work out” decreases the energy for closed systems
- Internal energy energy U consists of the kinetic energies and potential energies (e.g. molecular interactions) of all molecules in the system.

$$\Delta U = q - w$$

energy change heat added work done

The change in internal energy (ΔU) of all molecules in a closed system is equal to the heat added (q) to the system minus the work done by the system (w)



Enthalpy Definition

$$**H = U + PV** \qquad \mathbf{q = \Delta U + W} \text{ (1st law)}$$

where **U** is the total internal energy of the system (potential and kinetic);

P is pressure

V is the volume of the system

$$\Delta H = \Delta U + \Delta(PV)$$

Thermodynamic Processes

$$\Delta U = q - w$$

- Greek roots of the thermodynamic terms:
 - *isos* equal
 - *baros* weight
 - *adiabatos* not passable
- Isothermal $T = \text{const}$
- Isobaric $P = \text{const}$ $w = P\Delta V$ (*calorimetry*)
 $\Delta U + w = q$; $\Delta U + P\Delta V = q$; $\Delta(U + PV) = q$
- Isochoric $V = \text{const}$ $w = 0$ (*bomb calorimetry*), $\Delta U = q$
- Adiabatic $q = 0$ $\Delta U = -w$
- Enthalpy (or heat content) H is defined as $U + PV$, where P is pressure and V is volume.
- Heat content (H) of a drug specimen measured by a **calorimeter** helps to find states, transitions and temperature ranges of stability
- It also characterizes critical events like drug binding, amorphous drug compounds

Calorimetry and Heat Capacity

$$\Delta U = q - w$$

- We can measure heat (energy) $q = \Delta U + w$
 - transferred to the system, or
 - produced by the system

and associate it with temperature change of the system ΔT in a **calorimeter**

$$\text{Heat capacity, } C \equiv q / \Delta T$$

- Thus, the *heat capacity* of an object is defined as *the amount of heat energy required to raise its temperature by 1 K (or 1°C)*
- The heat capacity of *1 mol* of a substance is called its **molar heat capacity** Per mole: “molar”
- The heat capacity of *1 gram* of a substance is called its **specific heat** . Per gram: “specific”

reactions
physical changes



Caution about the sign of heat q : exothermic reaction implies **NEGATIVE heat value** (the system produced heat).

Heat Capacity at constant volume, C_V

$$\Delta U = q - w$$

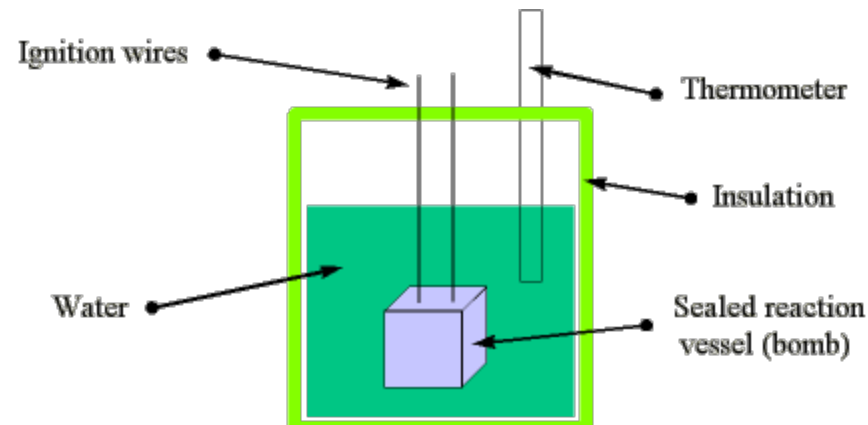
- At $V = \text{const}$, 1st law: $q = \Delta U$
- Bomb Calorimetry (constant-volume calorimetry)

- **Heat capacity** at constant volume

$$C_V \equiv \left(\frac{\partial U}{\partial T} \right)_V \cong \frac{q_V}{\Delta T}$$

- C_V values are tabulated.
- A practical relationship:

$$\Delta U \approx C_V \Delta T$$

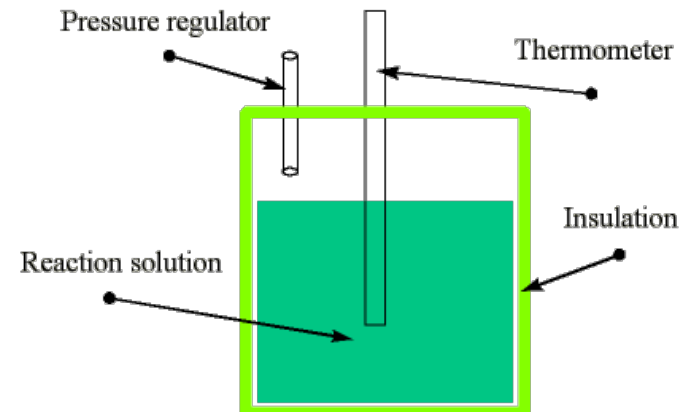


Heat Capacity at constant pressure, C_P

- Most processes in chemistry and biology occur at constant pressure
- Let us design a new function of state that is directly related to heat at constant pressure.
- Notice that at $P = \text{const}$

$$w = \int_a^b P dV = PV \Big|_a^b = PV_b - PV_a$$

$$q_p = \Delta U + P\Delta V \quad C_P = \frac{\Delta U + P\Delta V}{\Delta T}$$

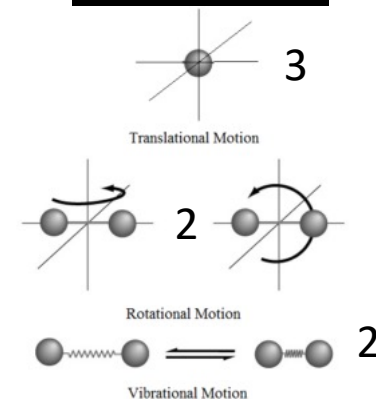
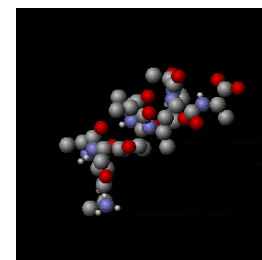


$$C_P \equiv \left(\frac{\partial(U + PV)}{\partial T} \right)_P \cong \frac{q_P}{\Delta T}$$

Understanding Heat Capacity from Atomic Structure

Degrees of Freedom of a Molecule in Gas

- Degrees of freedom (DF) store energy
- Number of DF increases with T (bonds get excited)
- Theory: $C_v = \frac{1}{2}R \times \text{number_of_DF}$; $C_p = C_v + R$
- In a drug molecule C_v is $R \times n_{\text{vibrational_DF}}$
- Monoatomic gas: 3 DF (translational), $C_v = 1.5R$
- Diatomic gas below vib. temp.: 5 DF (3 trans + 2 rot)
- Real values (25°C, 1 atm):



Monatomic gas	$C_{v,m}$ J/(mol·K)	$C_{v,m}/R$
He	12.5	1.5
Ne	12.5	1.5
Ar	12.5	1.5
Kr	12.5	1.5
Xe	12.5	1.5

Diatomic gas	$C_{v,m}$ J/(mol·K)	$C_{v,m}/R$
H ₂	20.18	2.427
CO	20.2	2.43
N ₂	19.9	2.39
Cl ₂	24.1	3.06
Br ₂ (vapor)	28.2	3.39

Enthalpy or Heat Content

- At $P = \text{const}$
- Calorimetry at constant pressure directly measures enthalpy increments, ΔH and C_P is ΔH_{1deg}
- to obtain $H(T_2)$, C_P can be integrated over T (Kirchhoff)
- H is a state function since U , P , and V are state functions

$$H = U + PV$$

$$\begin{aligned} q &= \Delta U + P\Delta V \\ &= \Delta(U + PV) \equiv \Delta H \end{aligned}$$

$$C_P \equiv \left(\frac{\partial H}{\partial T} \right)_P \cong \frac{q}{\Delta T}$$

$$\Delta H \approx C_P \Delta T$$

↑
(Kirchhoff)

Heats of Formation of a Molecule

- **Standard enthalpy of formation** of a compound is the change of enthalpy during the formation of 1 mole of the substance from its constituent elements (P=1bar, T usually 25 °C or 298.15 K)

- The $\Delta_f H^0$ values for most compounds are known. For example: [NIST Chemistry WebBook](#)

- Examples:

			$\Delta_f H^\ominus$ /(kJ/mol)
Ethanol	Liquid	C ₂ H ₅ OH	-277.0
Ethanol	Gas	C ₂ H ₅ OH	-235.3
Glucose	Solid	C ₆ H ₁₂ O ₆	-1271
Isopropanol	Gas	C ₃ H ₇ OH	-318.1

Enthalpy vs T: Kirchhoff's Law

Can we start from ΔH at T_1 and calculate ΔH at another temperature T_2 ?

By definition :

$$C_P \equiv \left(\frac{\partial H}{\partial T} \right)_P$$

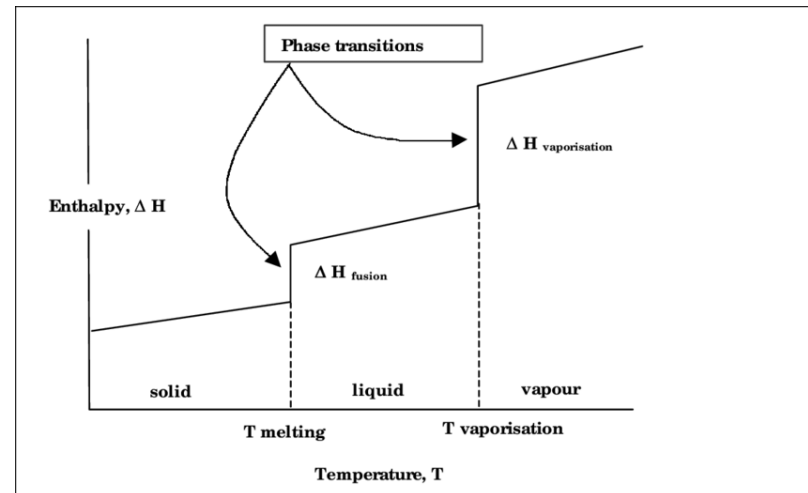
$$H(T_2) = H(T_1) + \int_{T_1}^{T_2} C_P dT$$

$$H(T_2) \approx H(T_1) + C_P \Delta T$$

The heat capacity itself depends on temperature, but near 270-370K in most biological reaction or transition cases we can assume $C_p = \text{const}$



Gustav Robert Kirchhoff,
1824-1887, a German physicist



Kirschhoff's Law: Example

- Enthalpy of formation of aspirin molecule is 736 kJ/mol at 298K and its heat capacity is 225 J/(mol K). Find ΔH and H at 36.6 C
- Solution:

$$H(T_2) \approx H(T_1) + C_p \Delta T$$

$$736 + 0.225 (36.6 - 25.0) \sim 739 \text{ kJ/mol}$$



Enthalpy and Internal Energy

$$\Delta H \approx \Delta U$$

- For *liquids and solids*

because the thermal expansion (volume change) is small.

- Even *if gas is produced* in a reaction, the extra 'work' is only:

$$H - U = PV = \mathbf{RT} = 2.5 \text{ kJ/mol} = 0.6 \text{ kcal/mol}$$

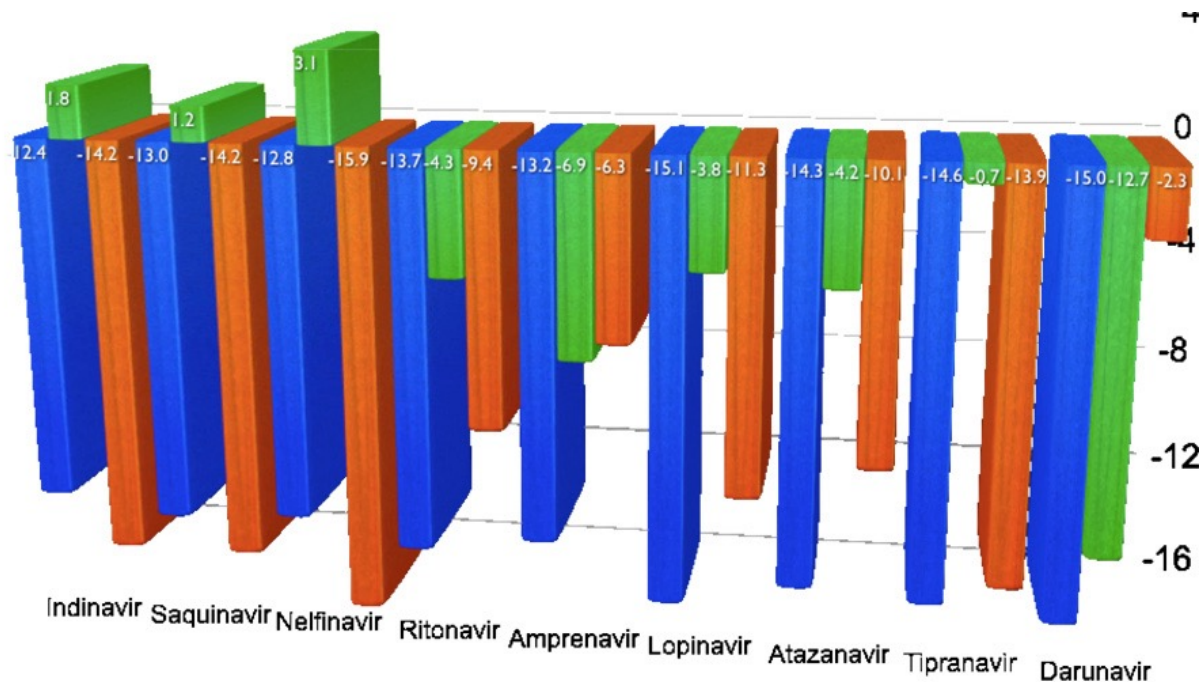
that is much smaller than a typical process or transition in liquids or solids (e.g. burning or dissolution, or partition)

- **Enthalpy** characterizes the internal energy changes (corrected by the pressure times volume change) in any of the *drug-related transitions*

Drug-Target Enthalpy of Binding

- An enthalpy difference between drug bound to the pocket and drug and pocket in solution (ΔH shown in green)

- Negative ΔH is better (specificity)



Summary

	Constant Volume	Constant Pressure
Defines	Heat at constant volume	Heat at constant pressure
Energy	Internal Energy, U	Enthalpy, $H=U+PV$
Contributions	<i>Total potential and kinetic energy</i>	<i>Total energy shifted by PV</i>
Heat Capacity (slope of H vs T)	$C_v = \frac{\partial U}{\partial T}$	$C_p = C_v + P \frac{\partial V}{\partial T}$
Ideal Gas	$C_v = 6_{or3or5}R/2 + Rn_{vibr}$	$C_p = C_v + R$
Energy Increments	$\Delta U \approx C_v \Delta T$	$\Delta H \approx C_p \Delta T$
Ground State	Only ΔU with respect to a described <i>ground state</i> (U_0) makes sense. C_v does not depend on U_0	Same for ΔH and C_p